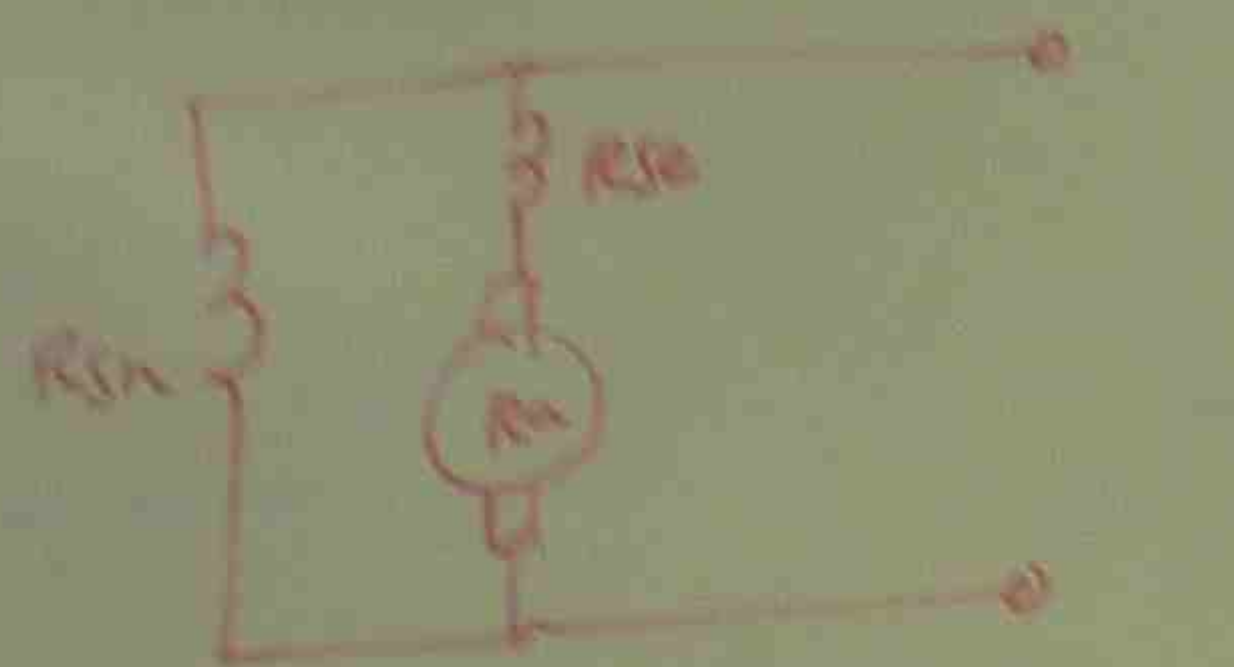


compound motor



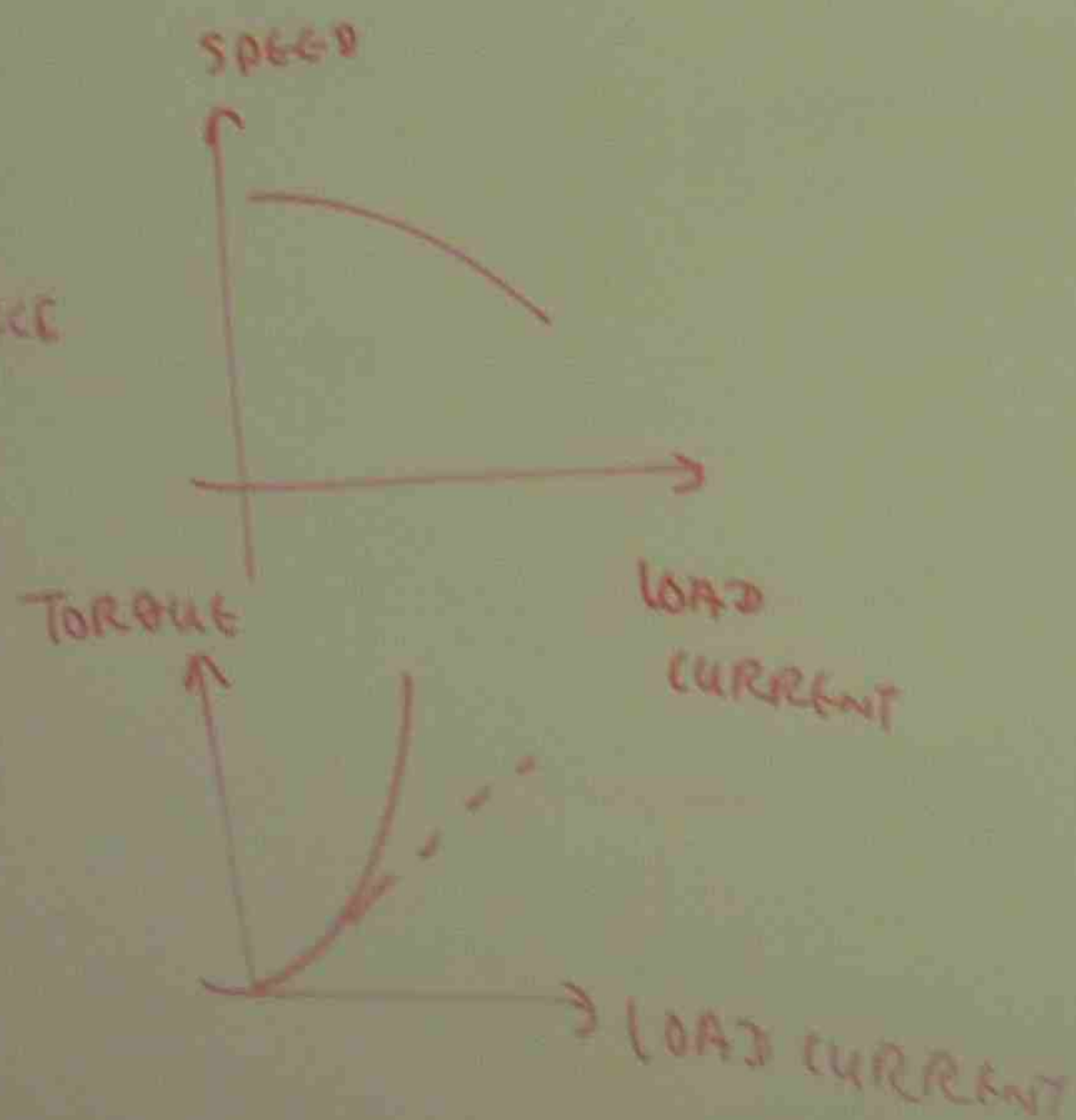
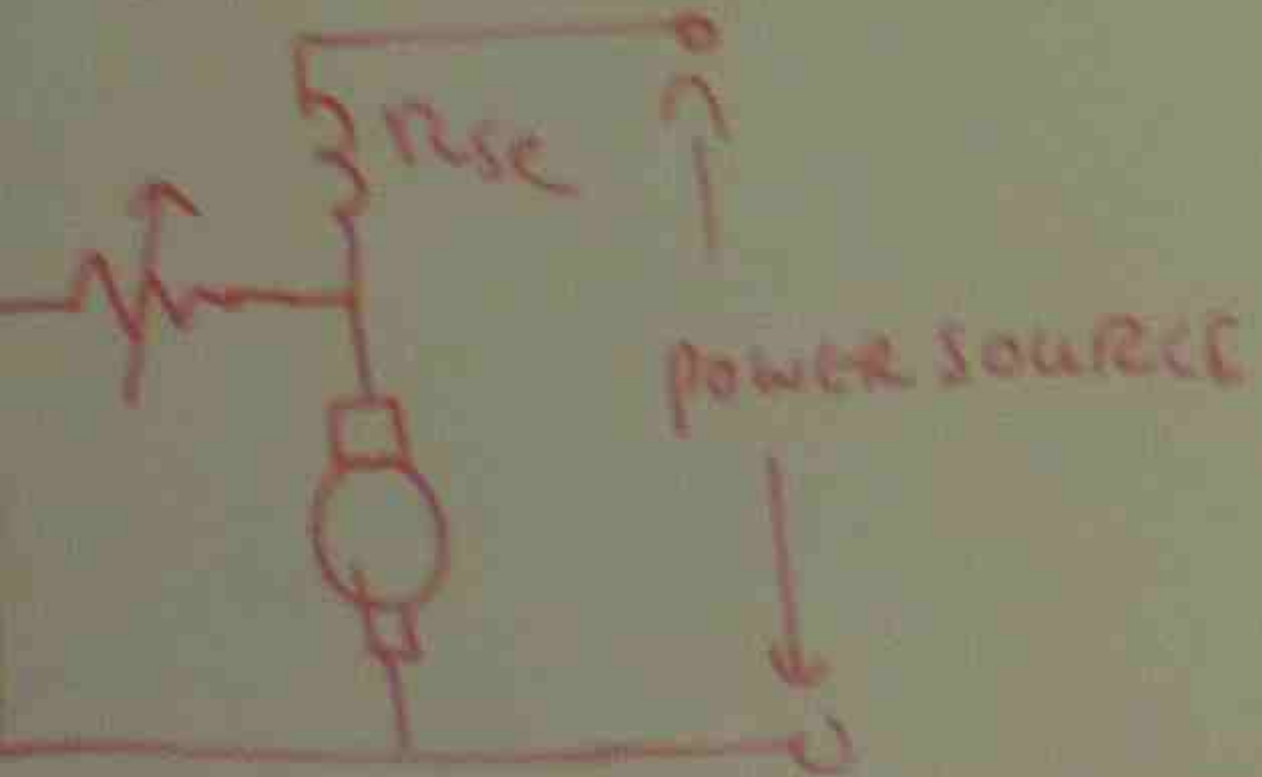
Short shunt compound



Long shunt compound

cumulative compound

cumulative compound machine combines the characteristics of both the series & shunt motor. Applications are punches, shears, rolling mills.



G043 + G044 + G045

Week 15

REVISION

8/11/11

Week 16

FINAL TEST

15/11/11

Week 17

ALL COME TO CLASS

22/11/11

- BRING BOTH ORANGE & YELLOW FORM

- SIGN RPL  
+  
ATTACH ANSWER PAPER

+  
PRESENT THE FORM TO  
H/T ALL TOGETHER.

+  
ATTENDANCE ROLL SHEET



## RELATING THE LINEAR AND ANGULAR VARIABLES

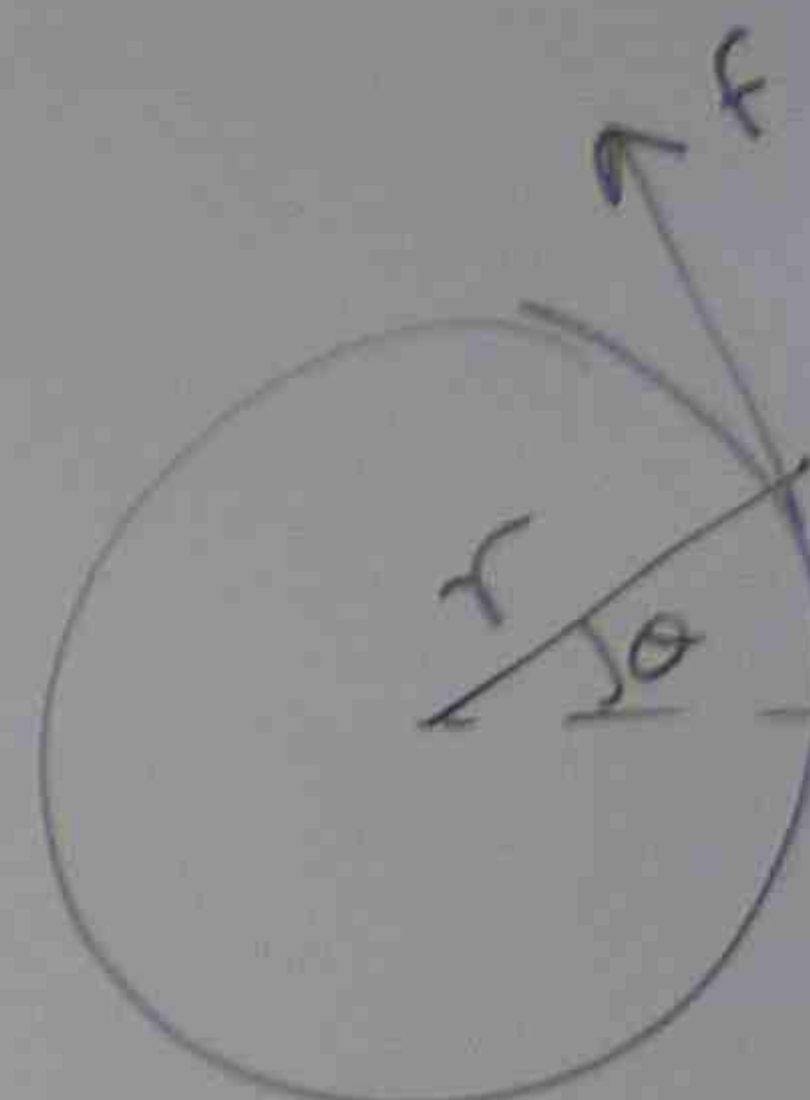
DISPLACEMENT

$$s = \theta r$$

$s$  = LINEAR DISPLACEMENT (m)

$\theta$  = ANGULAR DISPLACEMENT (Rad)

$r$  = RADIUS



THE SPEED

$$\frac{ds}{dt} = r \frac{d\theta}{dt}$$

$$v = \omega r$$

$v$  = LINEAR VELOCITY m/s

$\omega$  = ANGULAR VELOCITY RAD/s

$r$  = RADIUS OF CURVATURE (m)

ACCELERATION

$$\frac{dv}{dt}$$

$a$

$a$  = LINEAR ACCE

$r$  = RADIUS (

$\alpha$  = ANGULAR

$a_r$  = RADIAL



# ANGULAR VARIABLES

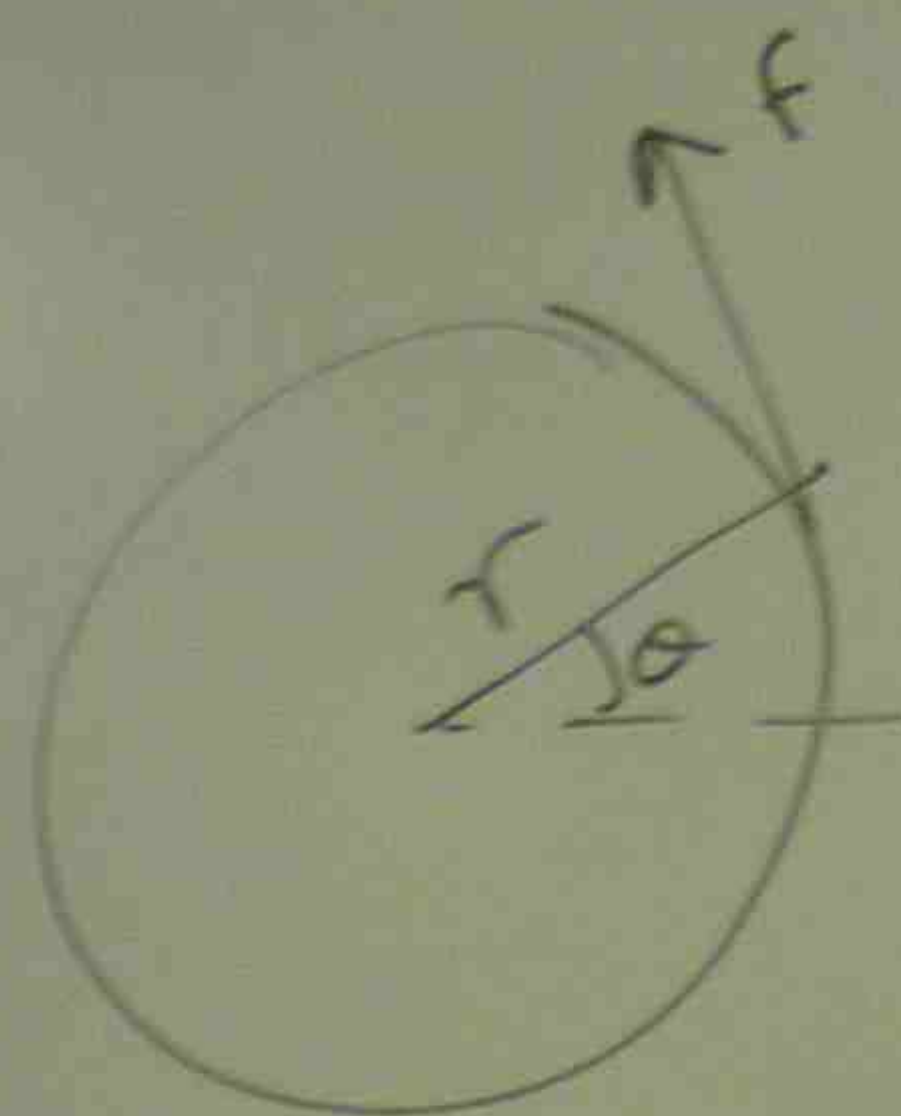
LENGTH (m)

ANGLE (Rad)

VELOCITY (m/s)

ANGULAR VELOCITY (RAD/s)

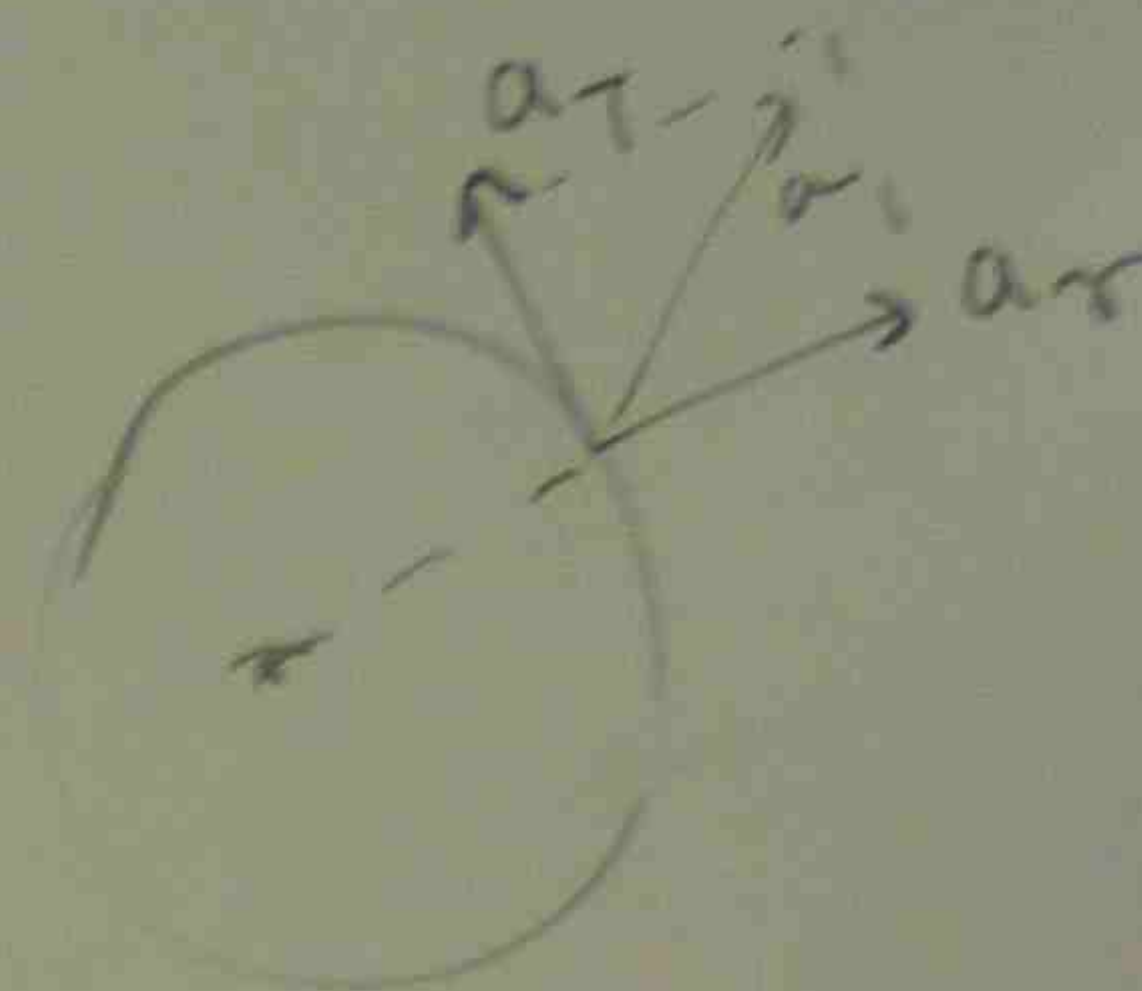
ACCELERATION (m/s<sup>2</sup>)



$$\tau = \frac{2\pi r}{v}$$

$\tau$  = TORQUE

$$\tau = \frac{2\pi}{\omega}$$



$$a_r = \frac{v^2}{r} = \omega^2 r$$

## ACCELERATION

$$\frac{dv}{dt} = r \frac{d\omega}{dt}$$

$$a_t = r \alpha$$

$a_t$  = TANGENTIAL ACCELERATION (m/s<sup>2</sup>) (TANGENTIAL)

$r$  = RADIUS (m)

$\alpha$  = ANGULAR ACCELERATION (RAD/s<sup>2</sup>)

$a_r$  = RADIAL ACCELERATION

ph

mech

3065

Co

SH

po

(a)

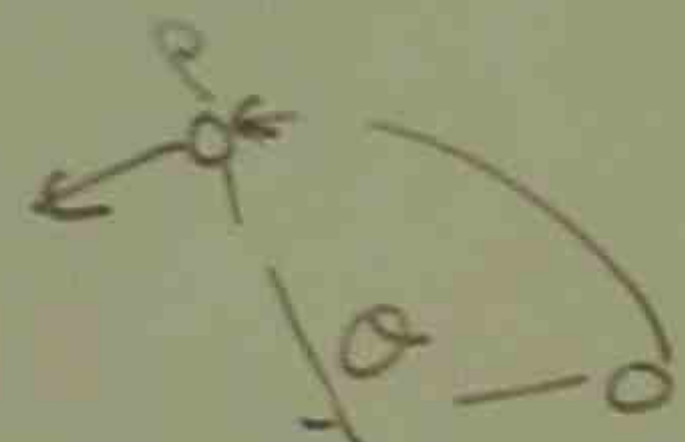
ANG

a-

a\_r



pb A COACH ROACH RIDES THE RIM OF A ROTATING MERRY GO ROUND. IF THE ANGULAR SPEED IS CONSTANT, DOES THE COACH ROACH HAVE (a) RADIAL ACCELERATION? (b) TANGENTIAL ACCELERATION? WHAT ANGLE  $\theta$  SHOULD THE ARC SUBTEND SO THAT  $a$  IS  $4g$  AT POINT 'P'



$$(a) a_T = \frac{dv}{dt} = r \frac{d\omega}{dt}$$

ANGULAR SPEED CONSTANT

$$\frac{d\omega}{dt} = 0$$

$$a_T = r \frac{d\omega}{dt} = r \times 0 = 0 \quad (b) \text{ NO TANGENTIAL ACCELERATION}$$

$$a_r = \omega^2 r \quad (a) \text{ IT HAS RADIAL ACCELERATION}$$

$$\omega^2 = \omega_0^2 + 2\alpha(\theta - \theta_0)$$

$$\alpha = \frac{a_T}{r}$$

$$\omega_0 = 0 \quad \theta_0 = 0$$

$$\omega^2 = 2\alpha\theta$$

$$\text{But } \alpha = \frac{a_T}{r}$$

$$\omega^2 = 2 \frac{a_T}{r} \theta$$

$$a_r = \omega^2 r$$

$$\omega^2 = \frac{a_r}{r}$$

$$\frac{a_r}{r} = 2 \frac{a_T}{r} \theta$$



$\theta - \theta_0$

$$a_r = 2 a_t \theta$$

$$a = \sqrt{a_t^2 + a_r^2}$$

$$\theta = \frac{1}{2} \sqrt{\frac{a^2}{a_t^2} - 1}$$

$$a = 4g \quad (\text{given})$$

$$a_t = g$$

$$\theta_p = \frac{1}{2} \sqrt{\frac{(4g)^2}{g^2} - 1}$$

$$= 1.94 \text{ RAD}$$

$$= 1.94 \times \frac{180}{\pi} = 111$$

$$a = \sqrt{a_t^2 + (2a_t\theta)^2} = a^2 = a_t^2 + (2a_t\theta)^2 = (2a_t\theta)^2 = a^2 - a_t^2$$

$$2a_t\theta = \sqrt{a^2 - a_t^2}$$

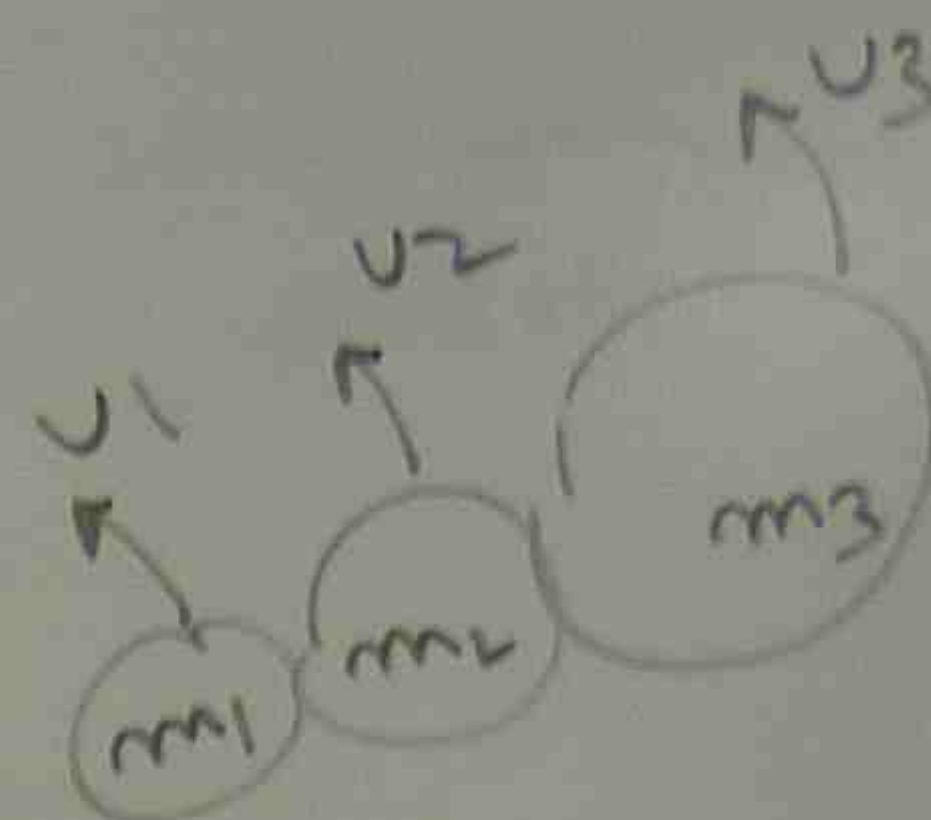
$$\theta = \frac{1}{2a_t} \sqrt{a^2 - a_t^2}$$

$$= \frac{1}{2} \sqrt{\frac{a^2}{a_t^2} - 1}$$

$$= \frac{1}{2} \sqrt{\frac{a^2}{a_t^2} - 1}$$

$$\begin{aligned}
 &= (2at\theta)^2 = a^2 - at^2 \\
 &2at\theta = \sqrt{a^2 - at^2} \\
 &\theta = \frac{1}{2at} \sqrt{a^2 - at^2} \\
 &= \frac{1}{2} \sqrt{\frac{a^2}{at^2} - 1} \\
 &= \frac{1}{2} \sqrt{\frac{a^2}{at^2} - 1}
 \end{aligned}$$

### KINETIC ENERGY OF ROTATION



$K =$  KINETIC ENERGY

$$\begin{aligned}
 K &= \frac{1}{2} m_1 v_1^2 + \frac{1}{2} m_2 v_2^2 + \frac{1}{2} m_3 v_3^2 \\
 &= \sum \frac{1}{2} m_i v_i^2
 \end{aligned}$$

$$v_i = \omega r_i$$

$$= \sum \frac{1}{2} m_i (\omega r_i)^2$$

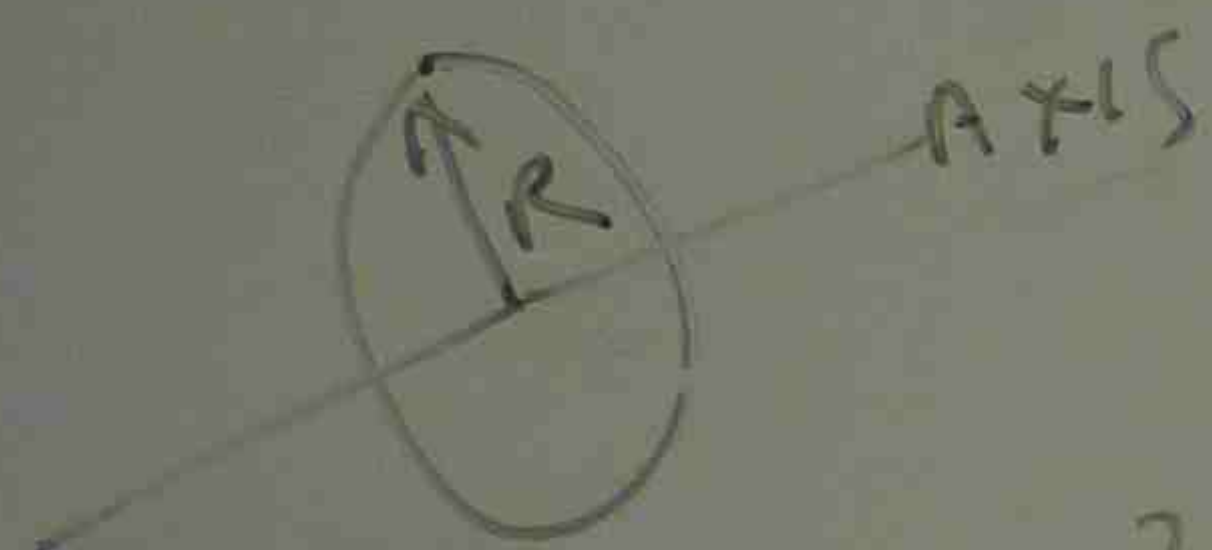
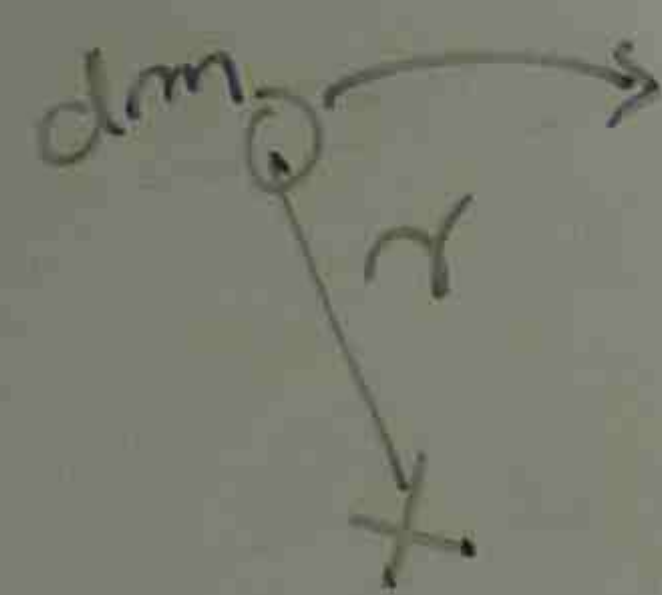
$$K = \frac{1}{2} \sum m_i r_i^2 \omega^2$$

ROTATIONAL INERTIA =  $I = \sum m_i r_i^2$

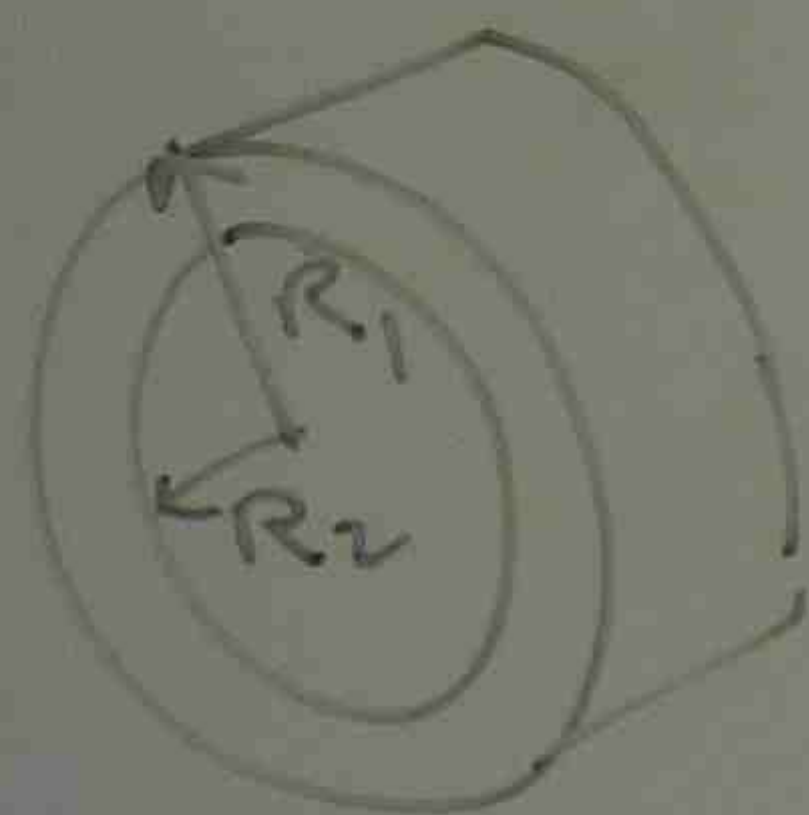
$$K = \frac{1}{2} I \omega^2$$



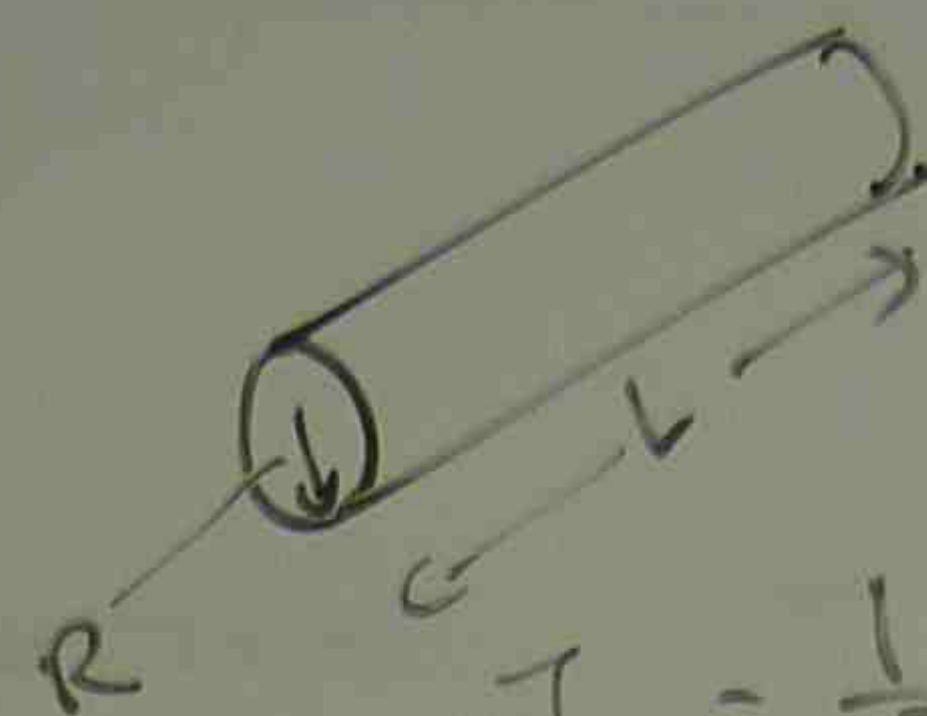
$$I = \int r^2 dm$$



$$I = m R^2$$



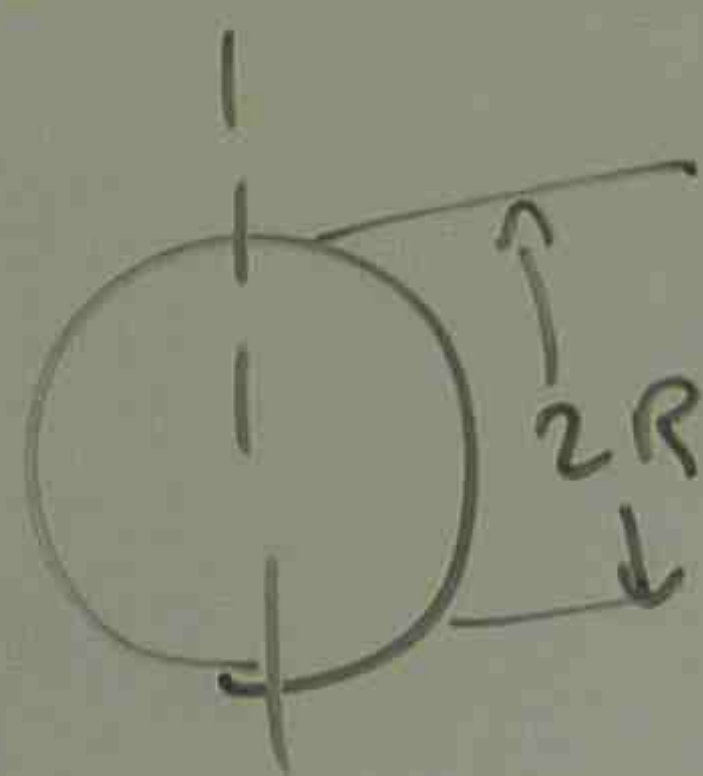
$$I = \frac{1}{2} m (R_1^2 + R_2^2)$$



$$I = \frac{1}{2} m R^2$$



$$I = \frac{1}{12} m L^2$$

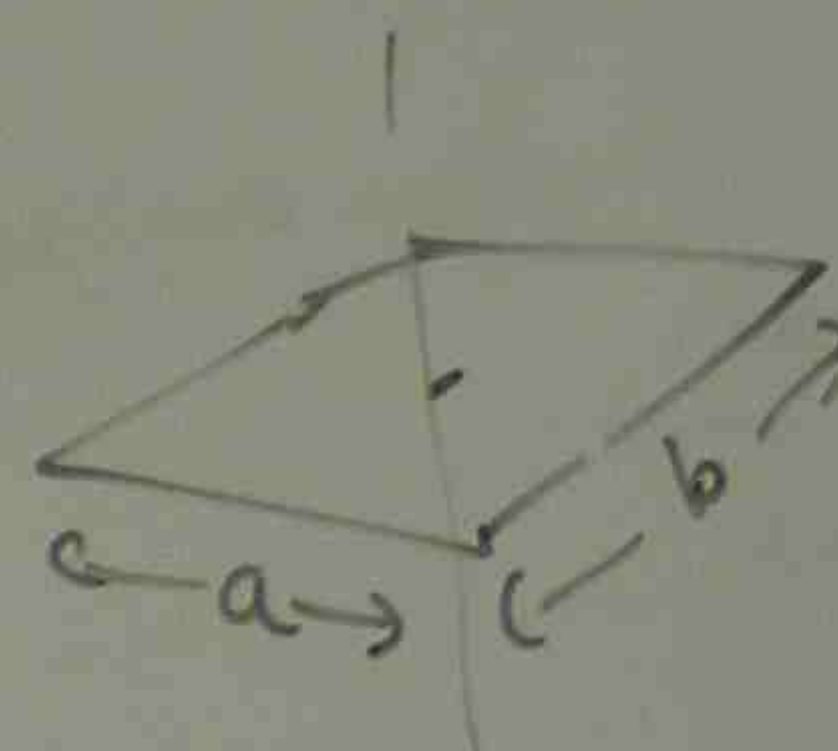


AXIS

$$I = \frac{2}{5} m R^2$$



$$I = \frac{1}{2} m R^2$$

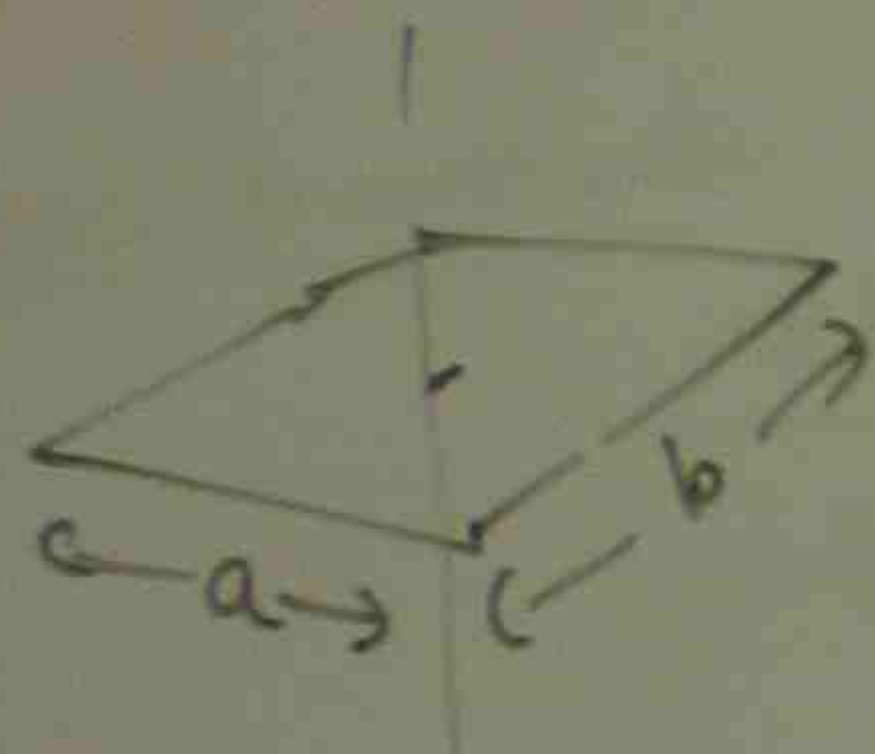


$$I = \frac{1}{12} m (a^2 + b^2)$$



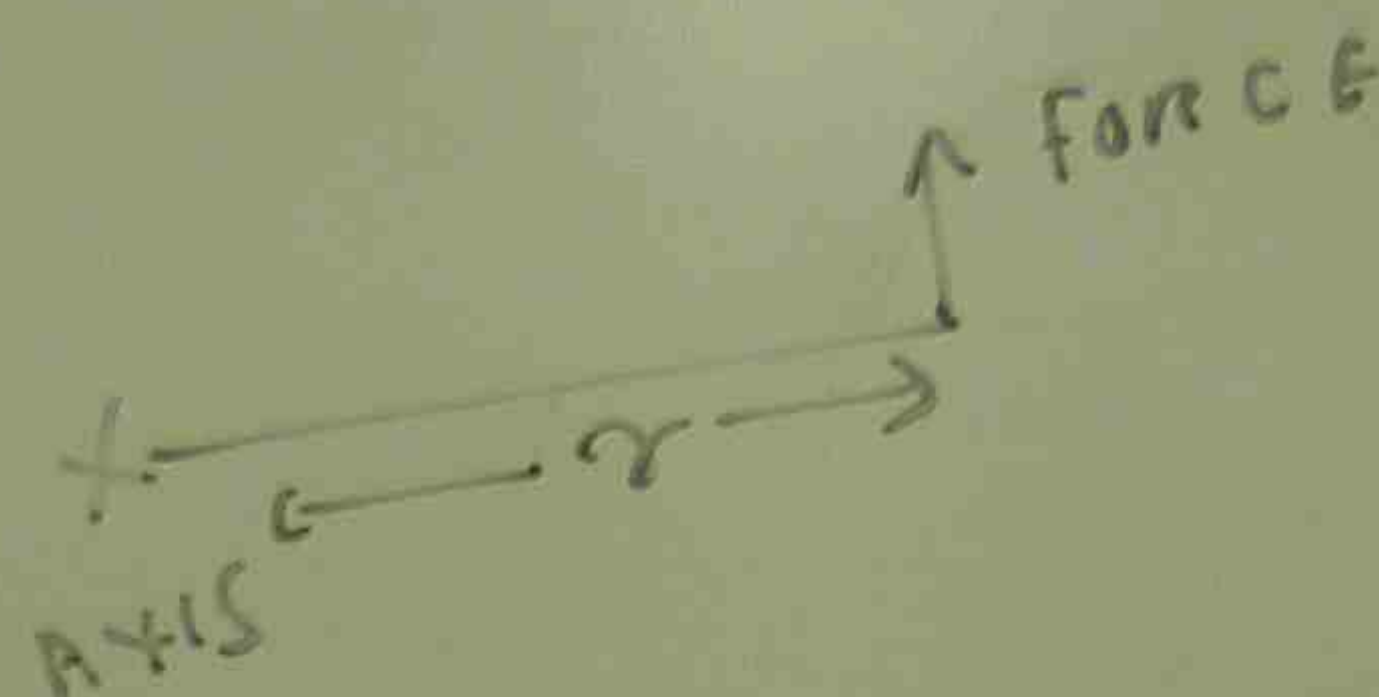


$$I = \frac{1}{2} m R^2$$



$$I = \frac{1}{12} m (a^2 + b^2)$$

## TORQUE



$$\text{Torque} = \text{FORCE} \times \text{DISTANCE}$$

$$T = F \times r \quad (\text{N-m})$$

$$T = I \alpha$$

$I$  = INERTIA

$\alpha$  = ANGULAR

ACCELERATION

$$T = m r^2 \alpha$$

pb

FIGURE SHOWS

$m = 2.5 \text{ kg}$

A BLOCK OF

A MASS LESS

OF FALLING

$T = m$

$a =$



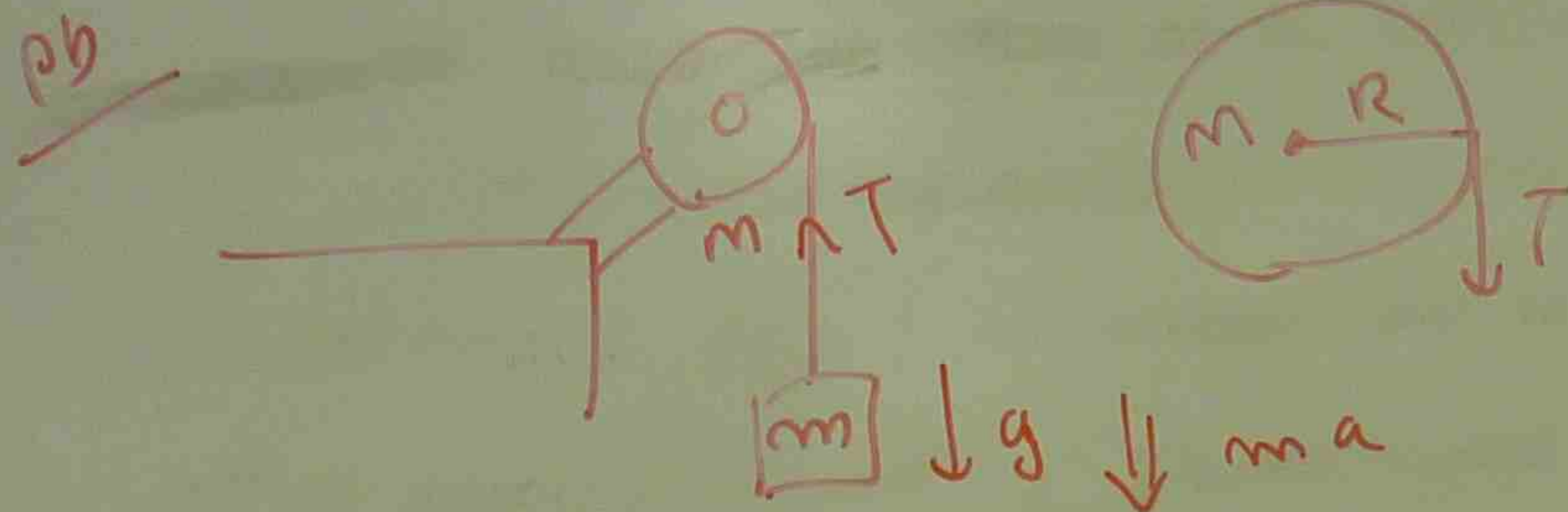


FIGURE SHOWS A UNIFORM DISK WITH MASS  $m = 2.5 \text{ kg}$ ,  $R = 20 \text{ cm}$ . A BLOCK OF  $m = 1.2 \text{ kg}$  HANGS FROM A MASS LESS CORD. FIND ACCELERATION OF FALLING BLOCK.

$$T = m \times R$$

$$T - mg = ma$$

$$a = \frac{T - mg}{m} = \frac{mR - mg}{m}$$

$$= \frac{2.5 \times \frac{20}{100} - 1.2 \times 9.81}{1.2}$$

$$a = \frac{0.5 - 1.2 \times 9.81}{1.2} = -9.39 \text{ m/s}^2$$



Diagram illustrating a pulley system. A pulley of mass  $m$  and radius  $R$  is shown. A string is draped over the pulley, with one end attached to a hanging mass  $m$ . The forces acting on the pulley are tension  $T$  from the string, weight  $mg$  downwards, and normal force upwards. The forces acting on the hanging mass are weight  $mg$  downwards and tension  $T$  upwards.

$$T = m \times R$$

$$T - mg = ma$$

$$a = \frac{T - mg}{m} = \frac{mr - mg}{m}$$

$$= 2.5 \times \frac{20}{100} - 1.2 \times 9.81$$

$$a = \frac{0.5 - 1.2 \times 9.81}{1.2}$$

$$= -9.39 \text{ m/s}^2$$