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CALCULATE THE KINETIC ENERGY, POTENTIAL ENERGY AND TOTAL ENERGY OF AN ELECTRON IN THE GROUND STATE OF A HYDROGEN ATOM.

GROUND STATE LEVEL ENERGY

TOTAL ENERGY = KINETIC ENERGY + POTENTIAL ENERGY

$$\frac{mv^2}{r} = \frac{e^2}{4\pi\epsilon_0 r^2}$$

$$KE = \frac{1}{2} mv^2$$

$$PE = -\frac{e^2}{4\pi\epsilon_0 r}$$

$$\frac{1}{2} mv^2 = \frac{1}{2} \frac{e^2}{4\pi\epsilon_0 r}$$

$$= \frac{1}{2} \times \frac{(1.6 \times 10^{-19})^2}{4 \times 3.14 \times 8.854 \times 10^{-12} \times 0.529 \times 10^{-10}}$$

$$= 2.175 \times 10^{-18} \text{ J}$$

$$1 \text{ eV} = 1.6 \times 10^{-19} \text{ J}$$

$$\frac{2.175 \times 10^{-18}}{1.6 \times 10^{-19}} = 13.6 \text{ eV}$$

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CALCULATE THE ENERGY AND RADII OF FIRST FOUR ORBITS FOR AN ELECTRON IN A HYDROGEN ATOM.

ENERGY

$$KE = \frac{1}{2} m v^2$$

$$PE = - \frac{e^2}{4\pi\epsilon_0 r^2}$$

$$TOTAL ENERGY = KE + PE = \frac{1}{2} m v^2 + \left( - \frac{e^2}{4\pi\epsilon_0 r^2} \right) \checkmark$$

$$m v r = \frac{n h}{2\pi}$$

$$v = \frac{n h}{m r n \pi}$$

$$\frac{1}{2} m v^2 = - \frac{e^2}{4\pi\epsilon_0 r^2}$$

$$\frac{1}{2} m \left[ \frac{n h}{m r n \pi} \right]^2 = - \frac{e^2}{4\pi\epsilon_0 r^2}$$

$$\frac{h}{2 r \pi} = - \frac{e^2}{4\pi\epsilon_0 r^2}$$

$$\frac{h}{2\pi} = - \frac{e^2}{4\pi\epsilon_0 r}$$

$$4\pi\epsilon_0 r h = - 2\pi e^2$$

$$r = \frac{- 2\pi e^2}{4\pi\epsilon_0 h} \checkmark$$



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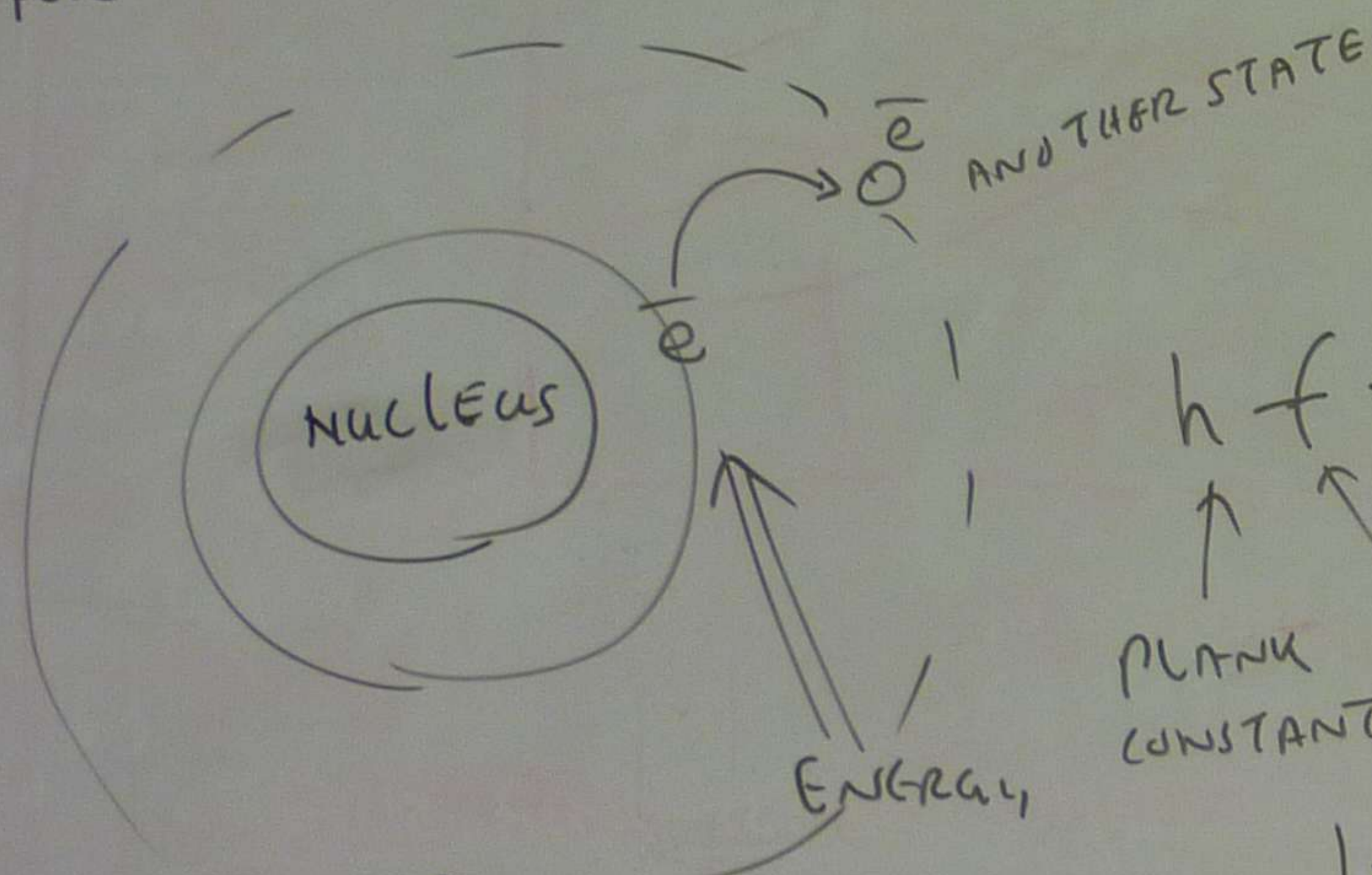
AN ELECTRON IN A HYDROGEN ATOM  
MAKES A TRANSITION FROM A QUANTUM  
STATE OF PRINCIPAL QUANTUM NUMBER  
 $n=2$  TO THE GROUND STATE. WHAT IS  
THE ENERGY AND WHAT IS THE FREQUENCY  
FOR EMITTED LIGHT QUANTUM.

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CHANGE OF STATE IS ASSOCIATED WITH  
ENERGY EMISSION

$$h f = |w_2 - w_1|$$

↑ PLANK CONSTANT      ↑ FREQUENCY

ENERGY CHANGE

$$w = \frac{-e^2}{8\pi\epsilon_0 r_1}$$

$$m v r = \frac{n h}{2\pi} \rightarrow v = \frac{n h}{2\pi m r}$$

$$\frac{1}{2} m v^2 = \frac{e^2}{8\pi\epsilon_0 r_1}$$

$$\frac{1}{2} m \left[ \frac{n h}{2\pi m r} \right]^2 = \frac{e^2}{8\pi\epsilon_0 r_1}$$

$$r = 529 \times 10^{-19} \text{ m}$$

$$\frac{m v^2}{r_1} = \frac{e^2}{4\pi\epsilon_0 r_1^2}$$

$$w = KE + PE$$

$$f' = \frac{|w_2 - w_1|}{h}$$

$$f = \frac{\left| -\frac{13.6}{2^2} - \left( -\frac{13.6}{1^2} \right) \right|}{8.254 \times 10^{-29}}$$

$$w_n = \frac{-e^2}{8\pi\epsilon_0 \times 0.529 \times 10^{-19}}$$

$$= -\frac{13.6}{n^2} \text{ eV}$$

$$w_1 = -\frac{13.6}{1^2}$$

$$w_2 = -\frac{13.6}{2^2}$$